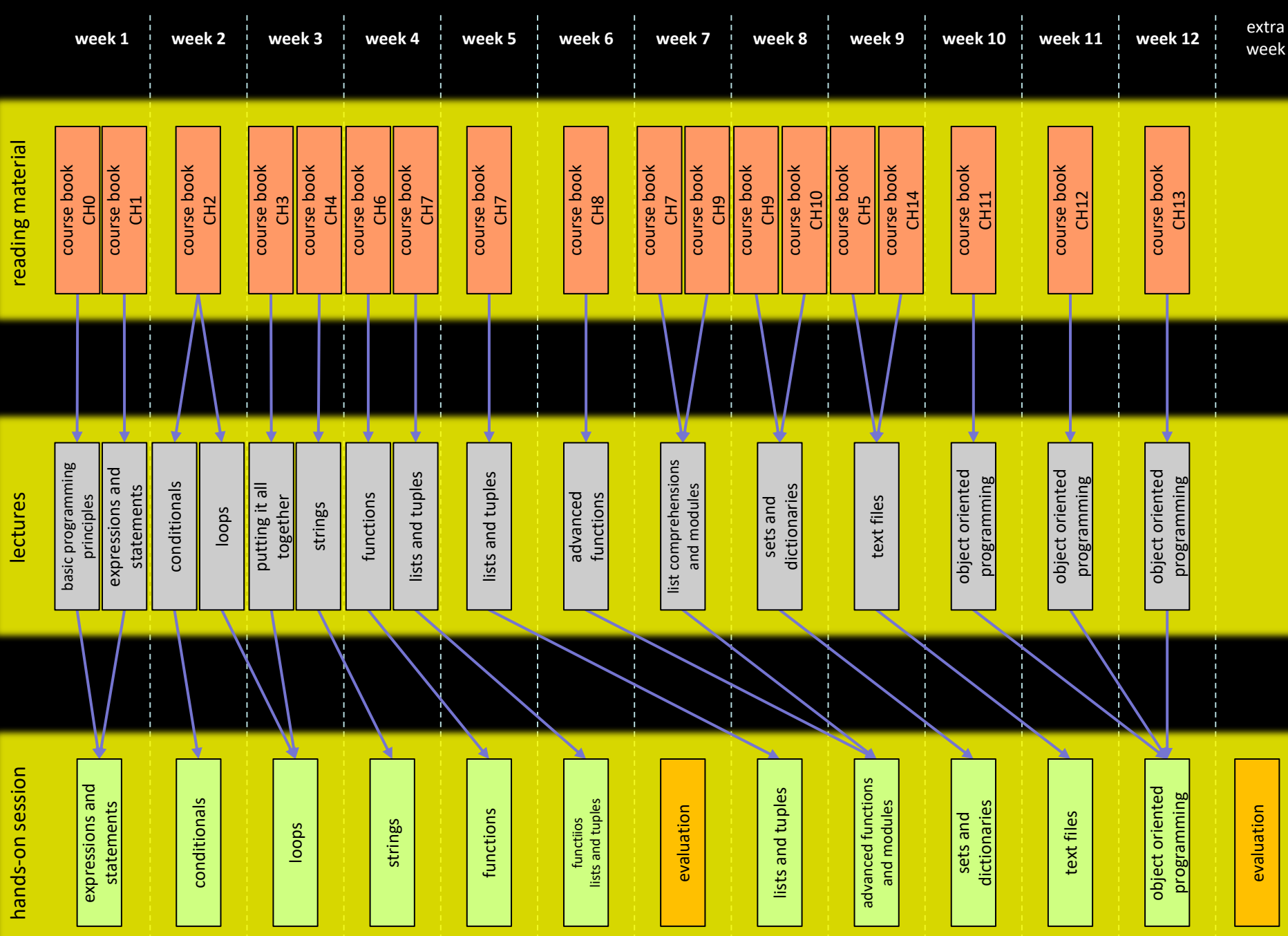




Prof. Dr. Peter Dawyndt

✉ peter.dawyndt@ugent.be

🐦 [@dawyndt](https://twitter.com/dawyndt)





What day is your birthday?

format: **DD/MM**

= two digits for day and month

= no year of birth

Example

I was born on December 5, 1975.

answer: **05/12**

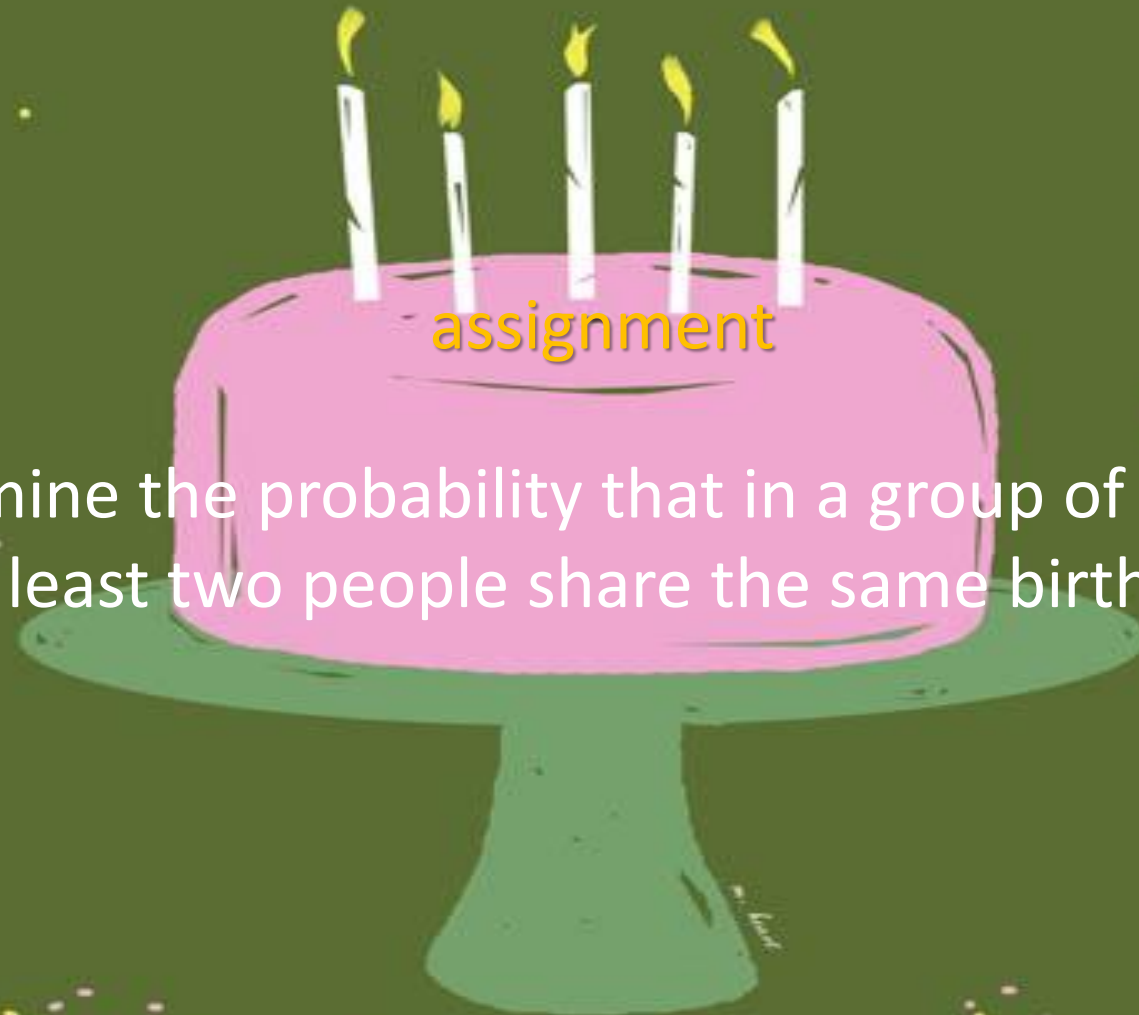


What is the probability that in this group of XX students, at least two students have their birthdays on the same day?

- A:** less than 10%
- B:** 10%-30%
- C:** 30%-50%
- D:** 50%-75%
- E:** more than 75%



the birthday paradox



Determine the probability that in a group of n people at least two people share the same birthday.



Birthday paradox



$$q_n = \frac{365}{365} \cdot \frac{364}{365} \cdot \frac{363}{365} \cdot \dots \cdot \frac{365 - n + 1}{365}$$

paradox1.py

```
for n in range(5, 76, 5):
    # compute probability
    qn = 1.0
    for m in range(n):
        qn *= (365 - m) / 365          # floating point division

    # print probability
    print(n, 1 - qn)
```



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Birthday paradox



$$q_n = \frac{365}{365} \cdot \frac{364}{365} \cdot \frac{363}{365} \cdot \dots \cdot \frac{365 - n + 1}{365}$$

paradox2.py

```
qn = 1.0
for n in range(2, 76):
    # compute probability
    qn *= (365 - n + 1) / 365          # floating point division

    # print probability
    if not n % 5:
        print(n, 1 - qn)
```



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Birthday paradox



$$q_n = \frac{365}{365} \cdot \frac{364}{365} \cdot \frac{363}{365} \cdot \dots \cdot \frac{365 - n + 1}{365}$$

paradox_graphical.py

```
import pylab
q_n = 365 / 365 * 364 / 365 * 363 / 365 * ... * 365 - n + 1 / 365
# construct graphical representation
x, y, qn = [], [], 1.0
for n in range(365):
    # compute probability
    qn *= (365 - n) / 365 # floating point division

    # add sample point
    x.append(n + 1) # x-value of sample point
    y.append(1 - qn) # y-value of sample point

# show graphical representation
pylab.plot(x, y, 'b-') # plot trend
pylab.xlim([0, 365]) # fix limits of x-axis
pylab.show() # show plot
```



Collatz Conjecture

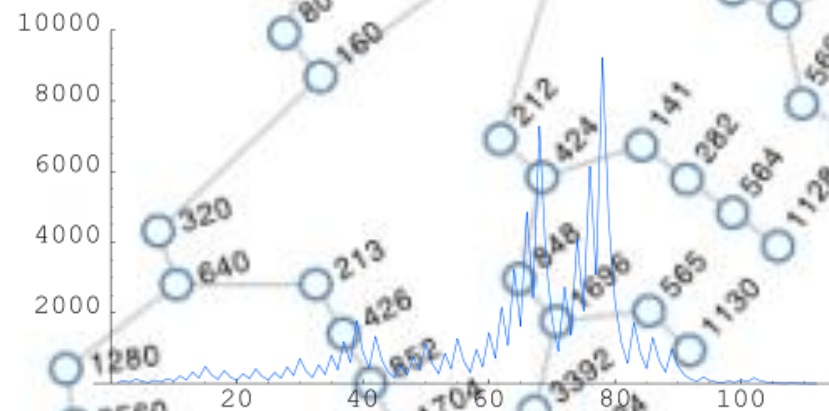


$$f(n) = \begin{cases} n/2 & \text{if } n \text{ is even} \\ 3n + 1 & \text{if } n \text{ is odd} \end{cases}$$

hailstone series:

$$a_i = \begin{cases} n & \text{voor } i = 0 \\ f(a_{i-1}) & \text{voor } i > 0 \end{cases}$$

27, 82, 41, 124, 62, 31, 94, 47, 142, 71, 214, 107, 322, 161, 484, 242, 121, 364, 182, 91, 274, 137, 412, 206, 103, 310, 155, 466, 233, 700, 350, 175, 526, 263, 790, 395, 1186, 593, 1780, 890, 445, 1336, 668, 334, 167, 502, 251, 754, 377, 1132, 566, 283, 850, 425, 1276, 638, 319, 958, 479, 1438, 719, 2158, 1079, 3238, 1619, 4858, 2429, 7288, 3644, 1822, 911, 2734, 1367, 4102, 2051, 6154, 3077, **9232**, 4616, 2308, 1154, 577, 1732, 866, 433, 1300, 650, 325, 976, 488, 244, 122, 61, 184, 92, 46, 23, 70, 35, 106, 53, 160, 80, 40, 20, 10, 5, 16, 8, 4, 2, 1



Collatz Conjecture



$$f(n) = \begin{cases} n/2 & \text{if } n \text{ is even} \\ 3n + 1 & \text{if } n \text{ is odd} \end{cases}$$

collatz.py

hailstone series:

$$a_i = \begin{cases} n & \text{voor } i = 0 \\ f(a_{i-1}) & \text{voor } i > 0 \end{cases}$$

```
cases = int(input())
for case in range(cases):
    # read start value and initialize cycle length
    n, cyclelength = int(input()), 1
    # determine length of hailstone series
    while n != 1:
        if n % 2:
            n = 3 * n + 1
        else:
            n //= 2
        cyclelength += 1
    # print length of hailstone series
    print(cyclelength)
```



Collatz Conjecture



collatz_graphical.py

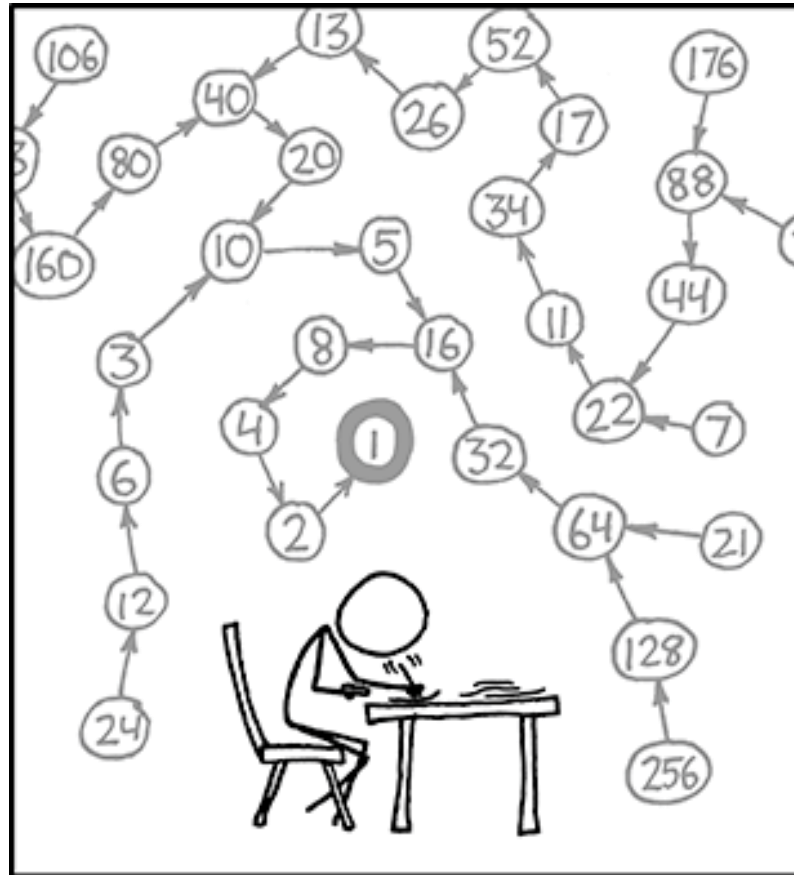
```
m = int(input('Enter a value for n: '))

# determine hailstone series
n = m
hailstone = [n]
while n != 1:
    if n % 2:                # n odd
        n = 3 * n + 1
    else:                    # n even
        n //= 2
    hailstone.append(n)

# graphical representation of hailstone series
import pylab
pylab.plot(range(1, len(hailstone) + 1), hailstone)
pylab.title(f'hailstone series for $n = {m}$')
pylab.xlim(1, len(hailstone))
pylab.xlabel('$i$')
pylab.ylabel('$a_i$')
pylab.show()
```



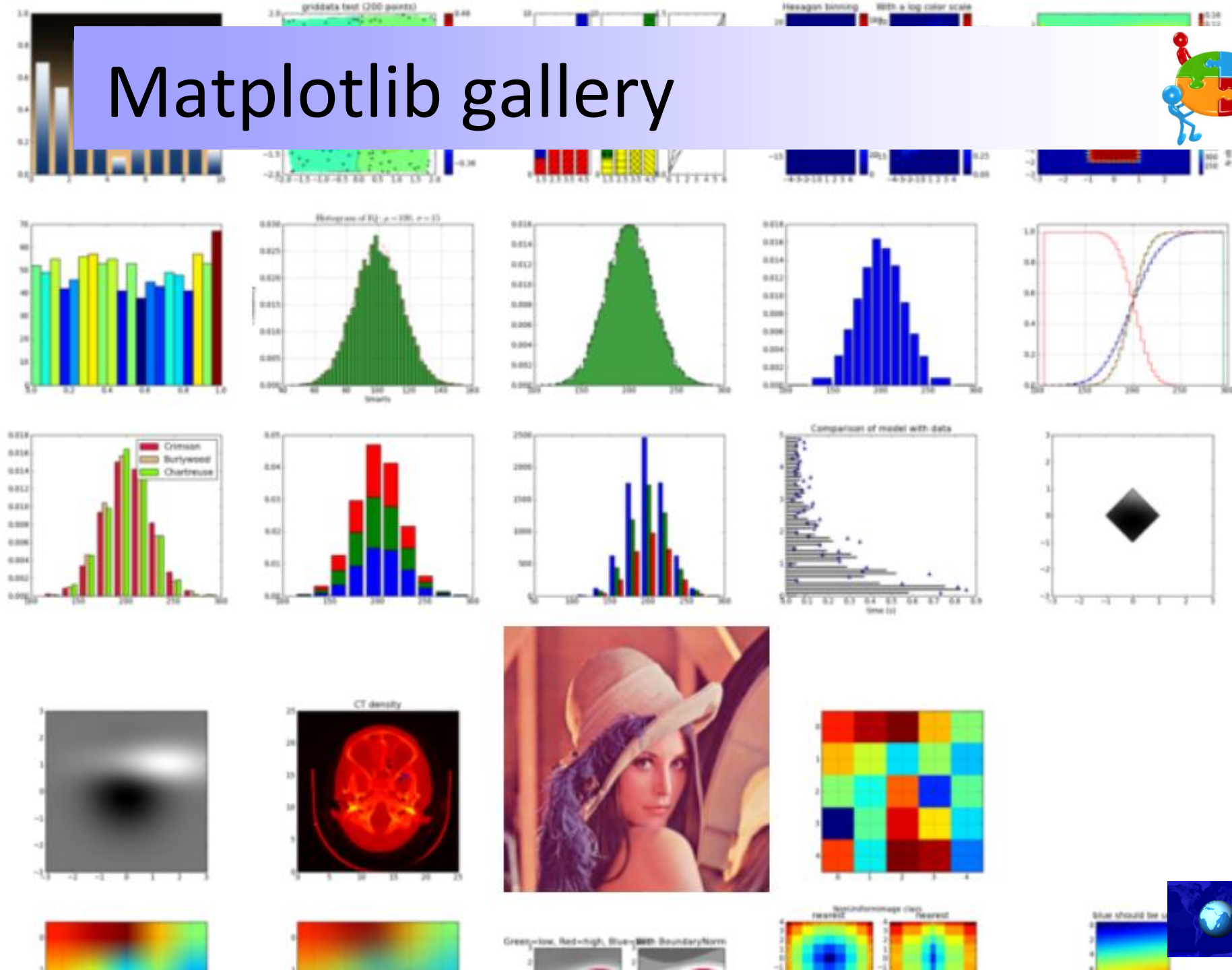
What's the use ?



THE COLLATZ CONJECTURE STATES THAT IF YOU PICK A NUMBER, AND IF IT'S EVEN DIVIDE IT BY TWO AND IF IT'S ODD MULTIPLY IT BY THREE AND ADD ONE, AND YOU REPEAT THIS PROCEDURE LONG ENOUGH, EVENTUALLY YOUR FRIENDS WILL STOP CALLING TO SEE IF YOU WANT TO HANG OUT.



Matplotlib gallery



For or while ?



```
#include <stdio.h>
int main(void)
{
    int count;

    for (count = 1; count <= 500; count++)
        printf("I will not throw paper airplanes in class.");
    return 0;
}
```

AVOND 10-3



```
printf("I will not throw paper airplanes in class.");
return 0;
}
```

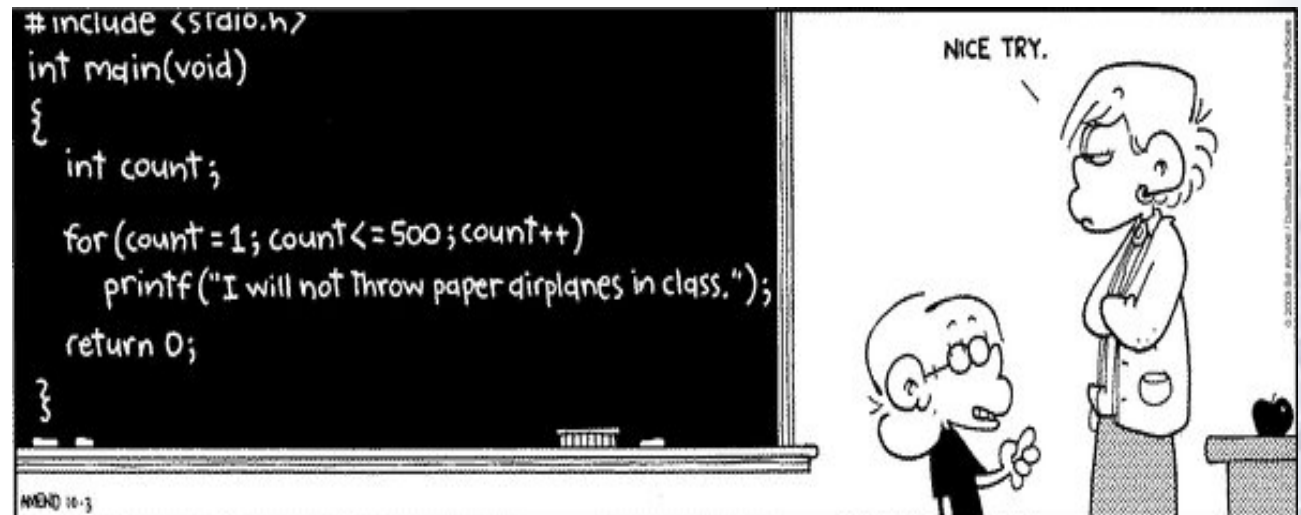
AVOND 10-3



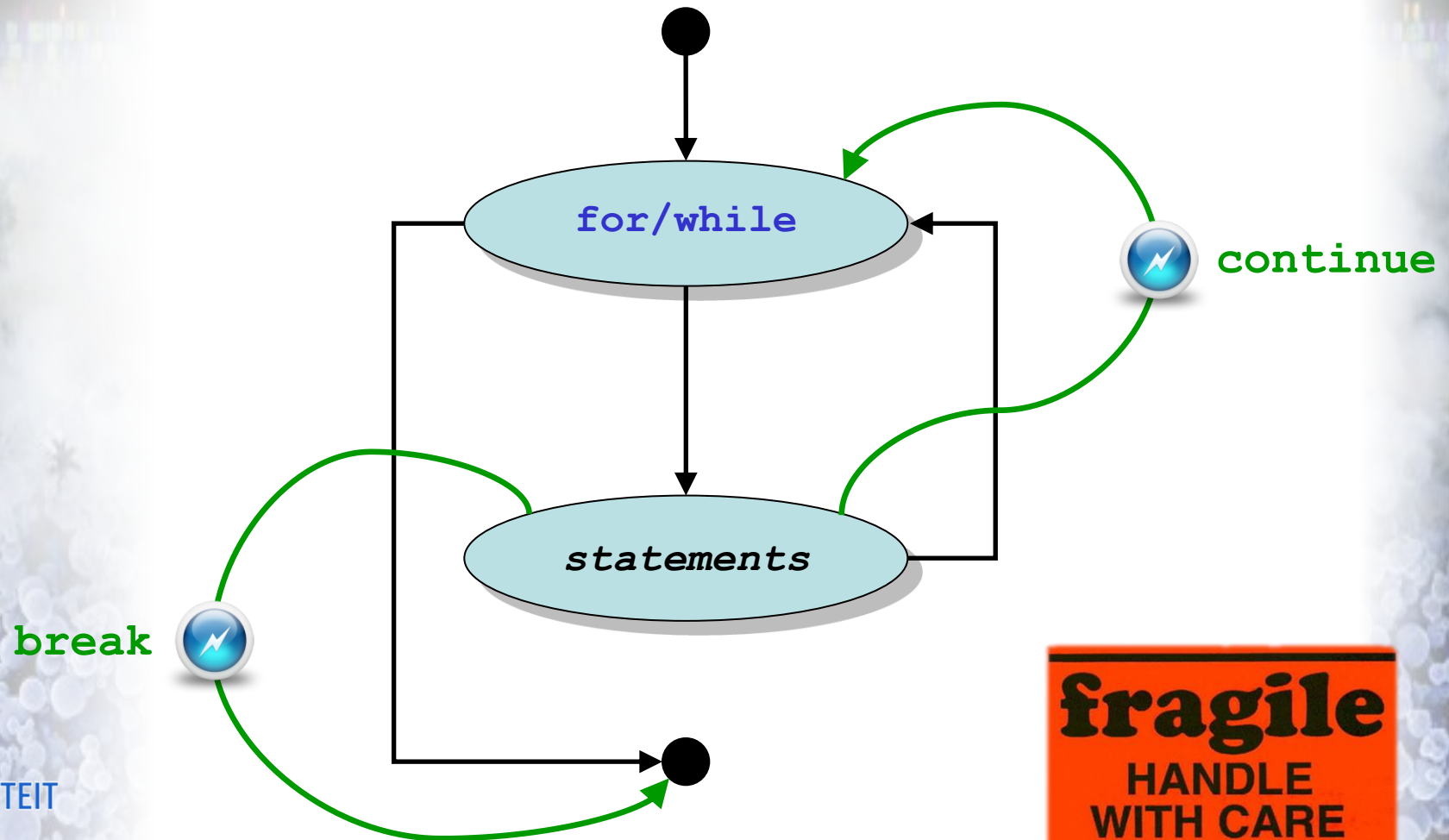
For or while ?



- for loops
 - number of iterations is **fixed** at the start of the loop
 - traversing elements of collection type using an iterator
- while loops
 - each iteration has an associated **condition** that determines whether or not a new iteration should be started



Short circuit



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Guess the number



guess1.py

```
# choose random number between 1 and 10 (limits included)
import random
number = random.randint(1, 10)

# give player three turns to guess the number
guessed = False
for attempts in range(3, 0, -1):

    # ask player to make a guess
    guess = int(input(f'Make a guess ({attempts} attempts left): '))

    # test if player has guessed the correct number
    if guess == number:
        print(f'Number guessed in {3 - attempts + 1} attempts!')
        guessed = True
        break
    else:
        print('Incorrect!')

# print correct number if not guessed by player
if not guessed:
    print(f'The number was {number}.')
```



Guess the number



guess1.py

```
# choose random number between 1 and 10 (limits included)
import random
number = random.randint(1, 10)

# give player three turns to guess the number
guessed = False
for attempts in range(3, 0, -1):

    # ask player to make a guess
    guess = int(input(f'Make a guess ({attempts} attempts left): '))

    # test if player has guessed the correct number
    if guess == number:
        print(f'Number guessed in {3 - attempts + 1} attempts!')
        guessed = True
        break
    else:
        print('Incorrect!')

# print correct number if not guessed by player
if not guessed:
    print(f'The number was {number}.')
```



Guess the number



guess2.py

```
# choose random number between 1 and 10 (limits included)
import random
number = random.randint(1, 10)

# give player three turns to guess the number
attempts, guessed = 3, False
while attempts and not guessed:

    # ask player to make a guess
    guess = int(input(f'Make a guess ({attempts} attempts left): '))
    attempts -= 1

    # test if player has guessed the correct number
    if guess == number:
        print(f'Number guessed in {3 - attempts} turns!')
        guessed = True
    else:
        print('Incorrect!')

# print correct number if not guessed by player
if not guessed:
    print('The number was {number}.')
```



Guess the number



guess3.py

```
# count number of attempts to guess a number between 1 and 100

# choose random number between 1 and 10 (limits included)
import random
number = random.randint(1, 100)

# allow player to guess the number until it is found
attempts, guess = 0, 0
while guess != number:

    # ask player to make a guess
    attempts += 1
    guess = int(input('What is your next guess? '))

    # hint about the number to be guessed
    if guess < number:
        print('Higher!!')
    elif guess > number:
        print('Lower!!')

# print number of attempts needed to guess the number
print(f'Number was guessed in {attempts} attempts.')
```



Series minimum and average



Write a program that computes the minimum and the average of a series of n integers.

```
$ python average.py < input.txt
minimum: 9
average: 22.875
$
```

43	12	33	15	23	37	11	9
----	----	----	----	----	----	----	---



min = 43 → 12 → 12 → 12 → 12 → 12 → 11 → 9
sum = 43 → 55 → 88 → 103 → 126 → 163 → 174 → 183



Series minimum and average



average.py

```
# determine minimum and average for a series of integers

# read length of series
n = int(input('Enter number of integers in series: '))

# initialize running variables
myMin = int(input('Enter first integer: '))
mySum = myMin

# traverse series
for i in range(n - 1):
    number = int(input('Enter next integer: '))
    mySum += number
    if number < myMin:
        myMin = number

# print minimum and average
print('minimum:', myMin)
print('average:', float(mySum) / n)
```



Closed series



Write a program that computes the sum of squares of a series of n integers.

$$\sum_{i=1}^n i^2$$

1	4	9	16	25	36	49	64
---	---	---	----	----	----	----	----



Closed series



Write a program that computes the sum of squares of a series of n integers.

$$\sum_{i=1}^n i^2$$

sum_closed_series.py

```
# read length of series
n = int(input('Enter number of integers in series: '))

# compute sum of squares
mySum = 0
for i in range(1, n + 1):
    mySum += i ** 2

# print sum of squares
print(f'The sum of the first {n} squares is {mySum}.')
```



Open series



Write a program that computes the sum of squares of a series of integers that ends with an empty input.

117	44	12	87	48	94	38	
-----	----	----	----	----	----	----	--



Open series



Write a program that computes the sum of squares of a series of integers that ends with an empty input.

sum_open_series.py

```
# compute sum of open series
mySum = 0
myInput = input('Enter next number (press [enter] to stop): ')
while myInput:
    mySum += int(myInput)
    myInput = input('Enter next number (press [enter] to stop): ')

# print sum of series
print(f'The sum of the numbers is {mySum}.')
```



Nested loops



Write a program that computes the result of the following double sum of series.

$$\sum_{i=1}^m \sum_{j=1}^n \frac{1}{i^2 + j^2}$$



Nested loops



Write a program that computes the result of the following double sum of series.

double_sum.py

```
# read limits
m = int(input('Enter value for m: '))
n = int(input('Enter value for n: '))

# compute double sum of series
mySum = 0.0
for i in range(1, m + 1):
    for j in range(1, n + 1):
        mySum += 1 / (i ** 2 + j ** 2)

# print sum
print(f'The double sum of the series is {mySum:.6f}.')
```



Fibonacci

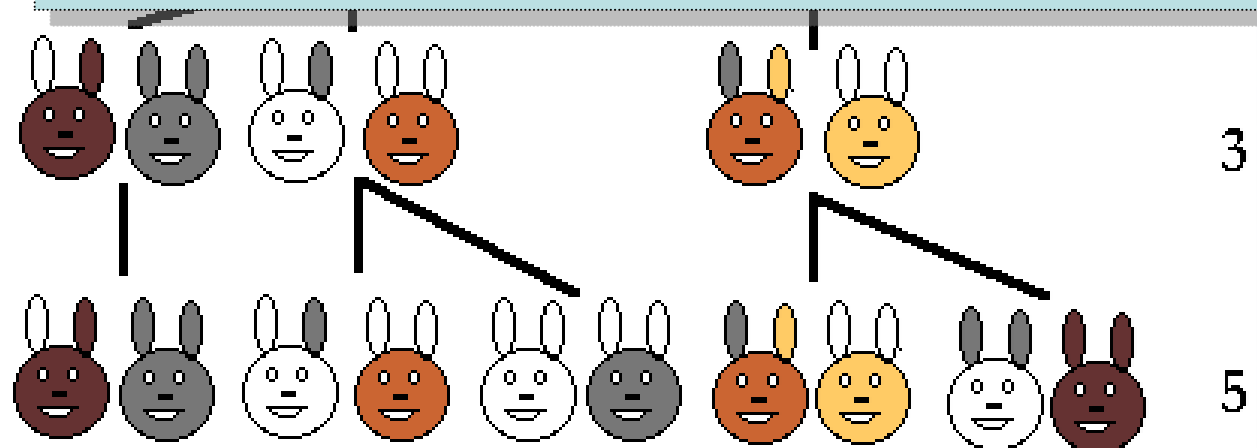


rabbit

Suppose a newly-born pair of rabbits, one male, one female, are put in a field. Rabbits are able to mate at the age of one month so that at the end of its second month a female can produce another pair of rabbits.

Suppose that our rabbits **never die** and that the female **always** produces one new pair (one male, one female) **every month** from the second month on. The puzzle that Fibonacci posed was...

How many pairs will there be in one year?



Fibonacci



Write a program that prints the first n numbers in the Fibonacci series.

$$\begin{cases} F_0 = 0 \\ F_1 = 1 \\ F_n = F_{n-1} + F_{n-2} \quad (n > 1) \end{cases}$$

fibonacci.py

```
# read value of n
n = int(input('Enter value of n: '))

# initialize and print first numbers
f0, f1 = 0, 1
print(f1)

# compute and print next number
for i in range(n - 1):
    f0, f1 = f1, f0 + f1
    print(f1)
```



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Fibonacci in nature



Head displaying florets in spirals
of 34 and 55 around the outside

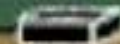


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Homework (next lecture)



- *course book*
 - *read chapter 4 (strings)*
 - *read chapter 6 (functions)*
- *read problem description of demo exercises*
 - *Caesar cipher*
 - *Letter soup*
 - *Toothpicks*
 - *Emirp*
 - *Sanger sequencing*
 - *Mobile synonyms*



Homework (hands-on sessions)



- mandatory exercises of series 03 (control loops)
(deadline Tuesday, October 14, 2025, 22:00)
 - ISBN (demo)
 - Chaos
 - German tanks
 - Monkeys and coconuts
 - Pythagorean triples
 - Hitchhikers problem



Questions or remarks ?



The sky is the limit ...



Lewis Carroll
1832-1898

"If you don't know where you are going,
any road will get you there."

— Lewis Carroll

